

SSC EXAM RELATED MATHEMATICS

Answers with Explanation

1. (c) $\frac{2}{3}\pi r_1^3 = 4 \cdot \frac{4}{3}\pi r_2^3$

$$\Rightarrow r_2^3 = \frac{1}{8} r_1^3$$

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$$\Rightarrow r_2 = \frac{1}{2} r_1$$

2. (b) L.C.M. (3, 5, 3) = 15

$$3 \rightarrow 40 \quad 5 \rightarrow 60$$

$$15 \rightarrow 200 \quad 15 \rightarrow 180$$

$$\text{Total C.P.} = 200 + 180 = 380$$

$$3 \rightarrow 50$$

$$3 \rightarrow 500 \text{ (S.P.)}$$

$$\text{Profit\%} = \frac{500 - 380}{380} \times 100\%$$

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$$= 31.57\% = 32\%$$

3 (b) Average = $\frac{4 \times 85 + 5 \times 87}{4 + 5} = 86.1$

4. (b) $\cot 41^\circ \cdot \cot 42^\circ \cdot \cot 43^\circ \cdot \cot 44^\circ \cdot \cot 45^\circ \cdot \cot 46^\circ$
 $\cdot \cot 47^\circ \cdot \cot 48^\circ \cdot \cot 49^\circ$
 $= \cot(90^\circ - 49^\circ) \cdot \cot(90^\circ - 48^\circ) \cdot \cot(90^\circ - 47^\circ)$
 $\cdot \cot(90^\circ - 46^\circ) \cdot \cot 45^\circ \cdot \cot 46^\circ \cdot \cot 47^\circ$
 $\cdot \cot 48^\circ \cdot \cot 49^\circ$
 $= \tan 49^\circ \cdot \tan 48^\circ \cdot \tan 47^\circ \cdot \tan 46^\circ \cdot \cot 45^\circ \cdot \cot 46^\circ$
 $\cdot \cot 47^\circ \cdot \cot 48^\circ \cdot \cot 49^\circ$
 $= 1.1.1.1.1 = 1$ [$\because \cot 45^\circ = 1$ and $\tan \theta \cdot \cot \theta = 1$]

5. (b) New average = $\frac{na + 2 + 4 + 8 + 16 + \dots + 2^n}{n}$

$$= \frac{na + 2 \left(\frac{2^n - 1}{2 - 1} \right)}{n} = a + 2 \cdot \frac{2^n - 1}{n}$$

6. (b) $\begin{array}{ccc} 40\% & & 100\% \\ & \searrow & \swarrow \\ & 50\% & \\ & \swarrow & \searrow \\ 50 & & 10 \end{array}$

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$$50 : 10 = 5 : 1$$

$$5 \rightarrow 300$$

$$1 \rightarrow \frac{300}{5} = 60 \text{ gm.}$$

7. (a) 60% of A = 30% of B

$$\Rightarrow A = \frac{1}{2} B \quad \dots (i)$$

$$B = 40\% C \quad \dots (ii)$$

$$C = x\% \text{ of A} \quad \dots (iii)$$

$$(i) A = \frac{1}{2} \times 40\% C$$

$$\Rightarrow A = \frac{1}{2} \times 40\% \times x\% \text{ of A}$$

$$\Rightarrow x = 500$$

8. (b) $\frac{x^2}{100}\%$ decreased = 4% decreased

9. (c) $x = \frac{\sqrt{13} + \sqrt{11}}{\sqrt{13} - \sqrt{11}}$

$$y = \frac{1}{x}$$

$$\therefore x = \frac{24 + 2\sqrt{13 \times 11}}{2}$$

$$= 12 + \sqrt{13 \times 11}$$

$$y = 12 - \sqrt{13 \times 11}$$

$$\therefore x + y = 24$$

$$3x^2 - 5xy + 3y^2$$

$$= 3x^2 + 6xy + y^2 - 11xy$$

$$= 3 \times 24^2 - 11$$

$$= 1717$$

10. (b) $\frac{90}{54} = \frac{120}{x}$

$$\Rightarrow x = ₹ 72$$

11. (c) $7\sin^2\theta + 3\cos^2\theta = 4 \Rightarrow 7\sin^2\theta + 3 - 3\sin^2\theta = 4$

$$\Rightarrow 4\sin^2\theta + 3 = 4 \Rightarrow \sin^2\theta = \frac{1}{4}$$

$$\Rightarrow \sin^2\theta = \frac{1}{2} = \sin^2 30^\circ \Rightarrow \theta = 30^\circ$$

$$\therefore \tan\theta = \tan 30^\circ = \frac{1}{\sqrt{3}}$$

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12. (b) $\Delta GBC = \frac{60}{3} = 20 \text{ cm}^2$

13. (a) Let the distance be D km.
- $$\frac{1}{4}D + \frac{3}{12}D = 7$$
- $$\Rightarrow \frac{D}{40} + \frac{D}{16} = 7$$
- $$\Rightarrow \frac{2D+5D}{80} = 7$$
- $$\Rightarrow 7D = 7 \times 80$$
- $$\therefore D = 80 \text{ km}$$
14. (a) $I = Pt \frac{r}{100}$
- $$\Rightarrow \frac{8}{25} = P \times \frac{r^2}{200}$$
- $$\Rightarrow r = 8$$
- 15 (c) 80% of cost price = 300
- $$\therefore \text{Cost price} = \frac{300}{80} \times 100 = ₹ 375$$
- Now, SP = ₹ 405
- $$\therefore \text{Profit percentage} = \frac{405-375}{375} \times 100$$
- $$= \frac{30}{375} \times 100 = 8\%$$
- 16 (c) $\frac{4}{3} \pi (1)^3 + \frac{4}{3} \pi (6)^3 = \frac{4}{3} \pi (9)^3 - \frac{4}{3} \pi (r)^3$
- $$\Rightarrow 1+216 = 729-r^3$$
- $$\Rightarrow r^3 = 512 = 8^3$$
- Thickness = 9 - 8 = 1 cm
17. (c) 0.67 - 0.33 = 0.34
18. (c) Let a = b = c = 1
- $$\therefore a^2b^2c^2 = 1$$
19. (d) Let $\theta = 45^\circ$
- $$\therefore \frac{\tan 60^\circ}{\tan 30^\circ} = 3$$
20. (b) 40% × 30% + 60% 50%
- $$= 12\% + 30\%$$
- $$= 42\%$$
21. (a) 2 → 5
- $$8 = 2^3 \rightarrow 3 \times 5 = 15 \text{ year}$$
22. (a) $x^2 + y^2 = a^2 + b^2$
23. (b) $\frac{162}{2x+8} = 6$

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$$\Rightarrow x = 9\frac{1}{2} \text{ km/h}$$

24. (c) $V = \sqrt{5(5-a)(5-b)(5-c)} h$

$$= \sqrt{27 \times 14 \times 7 \times 6 \times 9}$$

$$= \sqrt{3 \times 3 \times 3 \times 2 \times 7 \times 7 \times 2 \times 3 \times 9}$$

$$= 3 \times 3 \times 2 \times 7 \times 9 = 1134 \text{ cm}^3$$

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25. (b) $\frac{3}{4} : \frac{2}{5}$

$$15:8$$

26. (a) $12600 \times \frac{95}{100} \times \frac{98}{100} = ₹ 11730.60$

27. (d) $a-3 - \frac{1}{a-3} = 2$

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$$= \frac{330}{\sqrt{(2+\sqrt{3})^2 - \sqrt{(\sqrt{3}+1)^2}}} = \frac{330}{2+\sqrt{3}-\sqrt{3}-1}$$

$$= 8$$

$$\Rightarrow (a-3)^3 - \frac{1}{(a-3)^3} = 3 \times 2 + 8 = 14$$

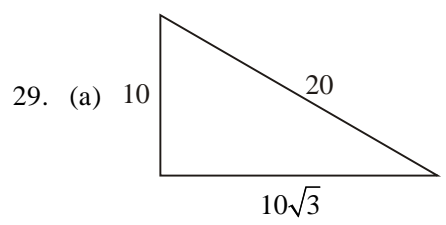
28. (d) $\frac{6^2+7^2+8^2+9^2+10^2}{\sqrt{7+4\sqrt{3}} - \sqrt{4+2\sqrt{3}}}$

$$= \frac{36+49+64+81+100}{\sqrt{2^2+(\sqrt{3})^2} + 2.2\sqrt{3} - \sqrt{(\sqrt{3})^2+1^2} + 2.1\sqrt{3}}$$

$$= \frac{330}{\sqrt{(2+\sqrt{3})^2 - \sqrt{(\sqrt{3}+1)^2}}} = \frac{330}{2+\sqrt{3}-\sqrt{3}-1}$$

$$= 330$$

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$$= \text{height} = 10 + 20 = 30$$

30. (d) $7 \times 1 = 7$

31. (c) $90 \times 16 \times 12 \times W = 70 \times 24 \times 8 \times 1$

$$\Rightarrow W = \frac{70 \times 24 \times 8 \times 1}{90 \times 16 \times 12} = \frac{7}{9}$$

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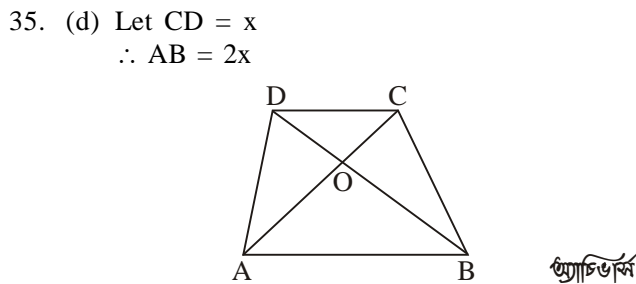
32. (a) Total S.A. = $\frac{1}{2} \times 4 \times 10 \times \sqrt{5^2 + 12^2} + 10^2$
 $= \frac{1}{2} \times 4 \times 10 \times 13 + 100$
 $= 260 + 100 = 360 \text{ cm}^2$

33. (c) Let $x = y = z$ অ্যাচিভার্স

$$\frac{3x^4 + 7y^4 + 5z^4}{5x^2y^2 + 7y^2z^2 + 3z^2x^2}$$

$$= \frac{3+7+5}{5+7+3} = 1$$

34. (a) $A + A \times 2 \times \frac{5}{100} = B + B \times 3 \times \frac{5}{100}$ অ্যাচিভার্স
 $= C + C \times 4 \times \frac{5}{100}$
 $\Rightarrow 22A = 23B = 24C = K$
 $\Rightarrow A = \frac{K}{22}, B = \frac{B}{23}, C = \frac{K}{24}$
 $A + B + C = 7930$
 $\Rightarrow K = 11 \times 23 \times 24 \times 10$
 $\therefore A = \frac{K}{22} = \frac{11 \times 23 \times 24 \times 10}{22}$
 $= 23 \times 12 \times 10 = 2760$

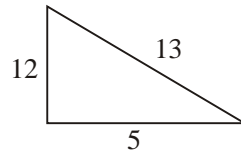


Now, $\frac{\text{Area of } \triangle AOB}{\text{Area of } \triangle COD} = \frac{AB^2}{CD^2}$
 $\Rightarrow \text{Area of } \frac{84}{\triangle COD} = \frac{4x^2}{x^2}$
 $\therefore \text{Area of } \triangle COD = \frac{84}{4} = 21 \text{ cm}^2$

36. (c) Speed of downstream = $\frac{60}{7.5} \times 1 = 8 \text{ km/h}$
 Speed of upstream = 5 km/h
 \therefore Speed of boat in still water
 $= \frac{8+5}{2} = \frac{13}{2} = 6\frac{1}{2} \text{ km/h}$ অ্যাচিভার্স

37. (c) We have, $A : B = 2 : 3$
 $B : C = 3 : 7$ অ্যাচিভার্স
 $\therefore A : B : C = 2 : 3 : 7$
 Let $A = 2K, B = 3K$ and $C = 7K$
 $\therefore A + B : B + C : C + A = (2K + 3K) : (3K + 7K) : (7K + 2K)$
 $= 5K : 10K : 9K = 5 : 10 : 9$

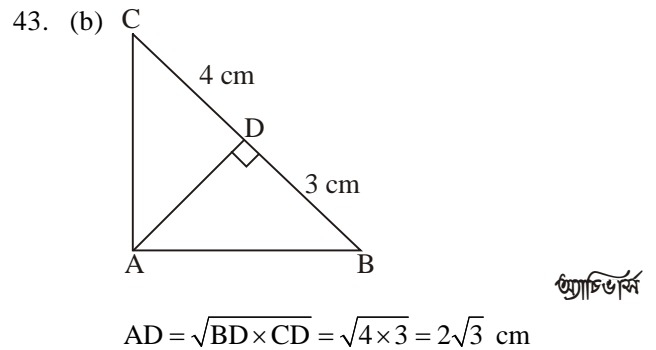
38. (b) $\sin \theta = \frac{12}{13}$



39. (a) $x = \sqrt{a} + \frac{1}{\sqrt{a}}, y = \sqrt{a} - \frac{1}{\sqrt{a}}$ অ্যাচিভার্স
 $x^2 = a + \frac{1}{a} + 2$
 $y^2 = a + \frac{1}{a} - 2$
 $(x^2 - y^2)^2 = 4^2 = 16$

40. (d) $(a+b)^3 - 3ab(a+b) - ab - (a+b)^2(a-b)^2$ অ্যাচিভার্স
 $= 1 - 3ab - ab - a^2 - b^2 + 2ab$
 $= 1 - 4ab + 2ab - \{(a+b)^2 - 2ab\} = 0$

41. (c) $m\% - n\% - \frac{mn}{100} = 10 - 10 - \frac{10 \times 10}{100} = -1\% \text{ loss}$
 42. (d) Given, $\sin A + \sin^2 A = 1$
 $\therefore \sin A = 1 - \sin^2 A = \cos^2 A$
 Now, $\cos^2 A + \cos^4 A = \cos^2 A + \sin^2 A = 1$



44. (c) Volume of ditch = $48 \times 16.5 \times 4$
 Volume of stone = $\pi(2)^2 \times 56$
 \therefore Portion to filled

$$= \frac{22}{7} \times 4 \times 56 = \frac{100}{48 \times 16.5 \times 4} = \frac{100}{450} = \frac{2}{9} \text{ part}$$

অ্যাচিভার্স

$$45. (a) 4 - \frac{5}{1 + \frac{1}{3 + \frac{1}{2 + \frac{1}{4}}}} = 4 - \frac{5}{1 + \frac{1}{3 + \frac{4}{9}}} = 4 - \frac{5}{1 + \frac{9}{31}}$$

$$= 4 - \frac{5 \times 31}{40} = \frac{32 - 31}{8} = \frac{1}{8}$$

46. (d) Let the exterior angle be x . অ্যাচিভার্স \therefore Interior angle = $x + 108^\circ$

$$\therefore x + x + 108^\circ = 180^\circ \Rightarrow 2x = 72^\circ$$

$$\Rightarrow x = 36^\circ$$

$$\therefore \text{Number of sides} = \frac{360^\circ}{36^\circ} = 10$$

47. (d) Let the number = $N = 361k + 47$ When $k = 1$, then $N = 408$

$$\therefore \frac{N}{19} = \frac{408}{19} = 9$$

48. (b) Radius of cylinder = 8 cm and height = 2 cm

 \therefore Volume of cylinder = Volume of cone

$$\Rightarrow \pi \times 8 \times 8 \times 2 = \frac{1}{3} \pi r^2 \times 6 \Rightarrow r^2 = 8 \times 8$$

$$\Rightarrow r = 8 \text{ cm} = \text{Radius of cone}$$

49. (a) Let the distance of D km.

$$\therefore \frac{D}{5} - \frac{D}{6} = \frac{12}{60} \Rightarrow \frac{6D - 5D}{30} = \frac{12}{60}$$

$$\Rightarrow D = 6 \text{ km}$$

অ্যাচিভার্স

50. (d) Let the total work = LCM of (16, 32, 48) = 96 units

 \therefore A's work = 6 units/day, B's work = 3 units/day and C's work = 2 units/dayLet the work be finished in x days.

$$\therefore 6x + 3(x - 8) + 2(x - 6) = 96$$

$$\Rightarrow 6x + 3x - 24 + 2x - 12 = 96$$

$$\Rightarrow 11x = 132$$

$$\Rightarrow x = 12 \text{ days}$$

$$51. (c) \frac{x+y}{x-y} = \left(\frac{3+2}{3-2} \right) = 5 \therefore 5:1$$

52. (b) Given, 50% of $x = 30\%$ of y

$$\Rightarrow \frac{x \times 50}{100} = \frac{y \times 30}{100}$$

$$\Rightarrow 50x = 30y$$

$$\Rightarrow 5x = 3y$$

$$\Rightarrow x : y = 3 : 5$$

অ্যাচিভার্স

$$53. (c) \frac{1}{\sqrt{2}+1} + \frac{1}{\sqrt{3}+\sqrt{2}} + \dots + \frac{1}{\sqrt{9}+\sqrt{8}}$$

$$= \sqrt{2}-1 + \sqrt{3}-\sqrt{2} + \dots + \sqrt{9}-\sqrt{8}$$

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$$= (\sqrt{9}-1) = (3-1) = 2$$

অ্যাচিভার্স

54. (a) Let the number be x

$$x^2 - 25 = (x - 25)^2$$

Put the option (a); then L.H.S = R.H.S

Then; answer is 13

55. (c) Given, number of armies member = 36562

Now,

	191	
1	3 65 62	
1	1	
29	265	
29	261	
381	462	
381	381	
	81	

অ্যাচিভার্স

Thus, after arrangement 81 armies were left.

56. (c) $72 = 9 \times 8$ (\therefore The question is in positive mode; then we should take maximum value) = 957. (b) Let Cow = x ; hen = y

$$x+y = 180 \rightarrow (i) \quad 4x+2y = 420 \rightarrow (ii)$$

$$\therefore 2x+2y = 360 \rightarrow (iii)$$

$$\therefore (ii) - (iii) \rightarrow 2x = 60$$

$$x = 30$$

58. (b) 6 can be written in the form of $n(n+1)$ ($n+2$)Let $n = 1$

Then,

$$6 = 1(1+1)(1+2)$$

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59. (d) $(11111)^2 = 123454321$

$$60. (b) \text{Earn/day} = \left(\frac{2000}{50} \right) = ₹40$$

Now \rightarrow Extra hours

$$= \frac{(2300-2000)}{(40+20)} = \left(\frac{300}{60} \right) = 5 \text{ hrs.}$$

$$61. (a) \frac{8 \times 4}{12} \times 60 = 160 \text{ mins.}$$

অ্যাচিভার্স

$$62. (c) \text{In } \rightarrow 1 \text{ hr. } \rightarrow x \text{ can copy} = \left(\frac{80}{20} \right) \text{ pages}$$

$$= 4 \text{ pages}$$

$$\therefore \text{In } \rightarrow 1 \text{ hr. } \rightarrow (x+y) \text{ can copy}$$

$$= \left(\frac{135}{27}\right) \text{ pages} = 5 \text{ pages} \quad \text{অ্যাচিভার্স}$$

∴ y can copy 1 page in 1 hr

∴ 20 page → 20 hrs.

63. (a) Let the CP of the motorcycle be ₹100x

$$\therefore \text{For Mr. x} = \left(90x \times \frac{108.5}{100}\right) \text{ and}$$

$$\text{For Mr. y} = \left(108.5x \times \frac{90}{100}\right)$$

∴ Same as the amount Mr. y paid

$$64. (b) Z = \left(x - y - \frac{xy}{100}\right) = 25 - 10 - \left(\frac{25 \times 10}{100}\right) = 12.5\%$$

65. (c) Price of each window অ্যাচিভার্স

$$= \left[\left\{ \left(120000 \times \frac{3}{4}\right) - 7500 \right\} \div 25 \right]$$

$$= (82500 \div 25) = ₹3300$$

66. (d) A : B = 3 : 2

B : C = 3 : 5

$$\hline A : B : C = 9 : 6 : 10$$

$$(A + B) : (B + C) = 15 : 16$$

67. (b) A : B

$$\left(x \times 10\right) + \left(\frac{3x}{4} \times 2\right) : \left(\frac{x}{2} \times 8\right) + \left(\frac{x}{4} \times 4\right)$$

$$\left(10 + \frac{3}{2}\right) : 5 = 23 : 10 \quad \text{অ্যাচিভার্স}$$

68. (c) A B C
(3×12):(5×12):(5×6)

$$= 6 : 10 : 5$$

69. (c) $63x^2 = 1575 \Rightarrow x^2 = 25 \Rightarrow x = 5$

$$\therefore \text{Max. no} = 9x = (9 \times 5) = 45$$

70. (d) Let the avg. of all 12 person be x kg.

$$\therefore (11 \times 95) + (x + 33) = 12x$$

$$\Rightarrow x = \left(\frac{1078}{11}\right) = 98$$

$$\therefore (98 + 33) = 131 \text{ kg.} \quad \text{অ্যাচিভার্স}$$

71. (c) According to the question, Largest number formed = 420

Smallest number formed = 204

$$\therefore \text{Required Average} = \frac{420 + 204}{2} = \frac{624}{2} = 312$$

$$72. (d) \frac{3^{30} + 3^{60} + 3^{90}}{3} = \frac{3^{30}(1 + 3^{30} + 3^{60})}{3} \quad \text{অ্যাচিভার্স}$$

$$= (3^{29} + 3^{59} + 3^{89})$$

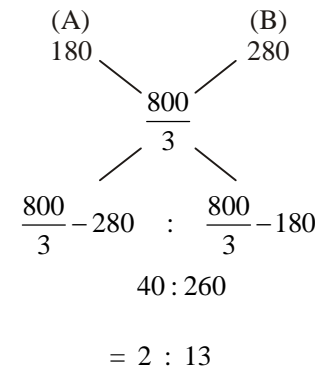
73. (c) Let CP = $\left(\frac{100}{80} \times 100x\right)$ [∵ MRP = 100x]

$$\text{Now, Profit} = \left(100x - \frac{250x}{4}\right) = \frac{150x}{4}$$

$$\therefore \text{Profit}(\%) = \left(\frac{150x}{4} \times \frac{4}{250x} \times 100\right)\% = 60\%$$

74. (b) Overall profit = 20% অ্যাচিভার্স

$$\therefore \text{CP of mixture} = \left(\frac{100}{120} \times 320\right) = ₹\left(\frac{800}{3}\right)$$



75. (d) $\frac{Q}{P} = \frac{96}{112} \Rightarrow Q : P = 6 : 7$ অ্যাচিভার্স

$$76. (b) \left(\frac{100 \times 100}{120 \times 75} \times P\right) = ₹\frac{10}{9}P$$

$$77. (c) \left[\left(\frac{30 - 25}{25}\right) \times 100\right]\% = \left(\frac{5}{25} \times 100\right)\% = 20\%$$

78. (c) Let use/day = 100x litres.

$$\therefore \left(\frac{3500x}{140x}\right) = 25 \text{ days} \quad \text{অ্যাচিভার্স}$$

79. (d) Let the greatest possible price be ₹x and the discount value is maximum

$$\therefore \text{By the condition} = \frac{3x}{4} = 270 \Rightarrow x = 360$$

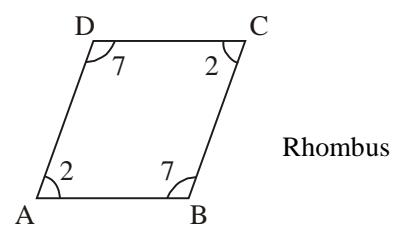
80. (b) $\frac{4 \times 16}{16-4} = \frac{4 \times 16}{12} = 5\frac{1}{3}$ hrs.
 81. (a) $P = \left(\frac{100 \times 1 \times 365}{5 \times 1}\right) = ₹ 7300$ প্র্যাচিভার্স

82. (c) Let the principal be ₹100x
 \therefore Interest = (10 + 10 + 1)% = 21%
 $\therefore 121x = 2420$
 $\Rightarrow x = 20 \Rightarrow 100x = ₹2000$

83. (b) Value of the ball = $\frac{4}{3}\pi CC$

84. (d) $C = 2\pi r \Rightarrow r = \frac{C}{2\pi}$ and $h = 4C$
 $V = \pi r^2 h = \left(\pi \cdot \frac{C^2}{4\pi} \times 4C\right) = \frac{C^3}{\pi}$

85. (b) opposite angle same = Rhombus প্র্যাচিভার্স



86. (d) $\left[\left(\frac{728}{2}\right) - \left(\frac{700}{2}\right)\right] = (364 - 350)m = 14m$

87. (a) Side of square
 $= \left(2 \times \frac{22}{7} \times 84 \times \frac{1}{4}\right) \text{ cm} = 132 \text{ cm.}$ প্র্যাচিভার্স

88. (c) Area increased = (5 + 5 + 0.25) = 10.25%

89. (b) $A_2 : A_1 = \left(\frac{3x}{2}\right)^2 : x^2 = \frac{9}{4} : 1 = 9 : 4$

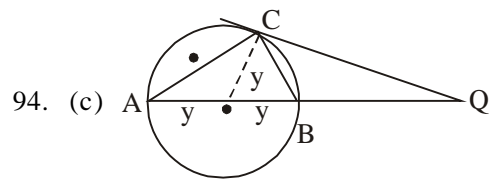
90. (d) $\frac{3-5x}{2x} + \frac{3-5y}{2y} + \frac{3-5z}{2z} = 0$
 $\Rightarrow \frac{3}{2x} + \frac{3}{2y} + \frac{3}{2z} - \left(\frac{5}{2} \times 3\right) = 0$
 $\Rightarrow \frac{1}{x} + \frac{1}{y} + \frac{1}{z} = \left(\frac{15}{2} \times \frac{2}{3}\right)$ প্র্যাচিভার্স
 $\Rightarrow \frac{2}{x} + \frac{2}{y} + \frac{2}{z} = 10$

91. (b) $(p+m)^3 - 3.pm(p+m) = 72$
 $\Rightarrow 6^3 - 18pm = 72$

$\Rightarrow pm = \left(\frac{216-72}{18}\right) = \left(\frac{144}{18}\right) = 8$

92. (b) $x^m \cdot x^n = 1 \Rightarrow x^{m+n} = x^0 \Rightarrow m+n=0$
 $\Rightarrow m = -n$

93. (d) $\therefore k = 2k - 1 \Rightarrow k = 1$ প্র্যাচিভার্স



$\angle CAB = 34^\circ$
 $CO = OA = \text{radius}$
 $\therefore \angle AC = 34^\circ$
 $\therefore \angle CAB = \left[\frac{180^\circ - (34 \times 2)}{2}\right] = \left(\frac{112}{2}\right) = 56^\circ$

95. (c) $2\sin^2\theta = 3\cos\theta$
 $2(1 - \cos^2\theta) = 3\cos\theta$
 $\Rightarrow 2 - 2\cos^2\theta = 3\cos\theta$ প্র্যাচিভার্স
 $\Rightarrow 2\cos^2\theta + 3\cos\theta - 2 = 0$
 $\Rightarrow \cos\theta = \frac{-3 \pm \sqrt{9+16}}{4} = \frac{-3 \pm \sqrt{25}}{4}$

Taking +ve sign, $\cos\theta = \frac{-3+5}{4} = \frac{2}{4} = \frac{1}{2}$
 $\Rightarrow \theta = 60^\circ$

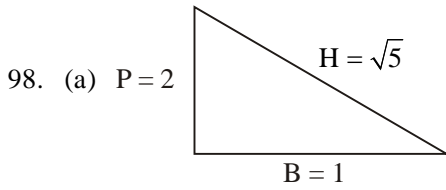
96. (c) Given, $3(\sec^2\theta + \tan^2\theta) = 5$
 $\Rightarrow 3(1 + \tan^2\theta + \tan^2\theta) = 5$ ($\because \sec^2\theta = 1 + \tan^2\theta$)
 $\Rightarrow 3 + 6\tan^2\theta = 5$
 $\Rightarrow 6\tan^2\theta = 2$
 $\Rightarrow \tan\theta = \frac{1}{\sqrt{3}}$
 $\Rightarrow \theta = 30^\circ$

$\therefore \cos 2\theta = \cos 60^\circ = \frac{1}{2}$

97. (d) $x \cdot \cos^2 60^\circ \sin 60^\circ = \frac{\tan^2 45^\circ \cdot \sec 60^\circ}{\operatorname{cosec} 60^\circ}$
 $\Rightarrow x \cdot \left(\frac{\sqrt{3}}{2}\right)^2 \cdot \frac{\sqrt{3}}{2} = \frac{(1)^2 \cdot 2}{\frac{2}{\sqrt{3}}}$

$\Rightarrow x \cdot \frac{3}{4} \cdot \frac{\sqrt{3}}{2} = \sqrt{3}$ প্র্যাচিভার্স

$\Rightarrow x = \frac{8}{3\sqrt{3}} \cdot \sqrt{3} = 2\frac{2}{3}$



$$\therefore \operatorname{cosec} \alpha = \frac{\sqrt{5}}{2} \text{ and } \sec \alpha = \frac{\sqrt{5}}{1} \quad \text{প্র্যাক্টিস}$$

\therefore Putting the value of $\operatorname{cosec} \alpha$ and $\sec \alpha$

$$= \frac{\left(\frac{\sqrt{5}}{2}\right)^2 - (\sqrt{3})^2}{\left(\frac{\sqrt{5}}{2}\right)^2 + (\sqrt{3})^2} = \frac{\left(\frac{5}{4} - 3\right)}{\left(\frac{5}{4} + 3\right)}$$

$$= \left(\frac{-\frac{7}{4}}{\frac{17}{4}}\right) \Rightarrow -\left(\frac{7}{17} \times \frac{4}{4}\right) = -\frac{7}{17} \quad \text{প্র্যাক্টিস}$$

99. (d) $\sin(\theta + 30^\circ) = \frac{3}{\sqrt{12}} = \frac{\sqrt{3}}{2} \left[\because \sin 60^\circ = \frac{\sqrt{3}}{2} \right]$

$$\Rightarrow \sin(\theta + 30^\circ) = \sin 60^\circ \quad \text{প্র্যাক্টিস}$$

$$\Rightarrow \theta + 30^\circ = 60^\circ \Rightarrow \theta = 30^\circ$$

$$\therefore \cos^2 \theta = \cos^2 30^\circ = \left(\frac{\sqrt{3}}{2}\right)^2 = \frac{3}{4}$$

100. (a) Angel shown by the students who go to institute on foot

$$= 360^\circ - (216^\circ + 54^\circ + 18^\circ) \quad \text{প্র্যাক্টিস}$$

$$= 360^\circ - 288^\circ = 72^\circ$$

\therefore Required number of students

$$= \frac{72^\circ}{360^\circ} \times 800 = 160$$

